

# $p\rho T_x$ -Property Measurements Near Saturation in the Gaseous Phase for Propane + Isobutane

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$p\rho T_x$ -property measurements near saturation in the gaseous phase for propane (1) + isobutane (2) at  $x_1 = 0.25$  ( $w_1 = 20.19\%$ ),  $x_1 = 0.5$  ( $w_1 = 43.14\%$ ), and  $x_1 = 0.80$  ( $w_1 = 75.22\%$ ) are reported. The data near saturation in the gaseous phase are important information for deriving reliable property values such as specific heats near saturation or for determining the second and third virial coefficients. The measurements were performed using a magnetic suspension densimeter. 154  $p\rho T_x$  values for propane + isobutane mixtures were obtained at the temperatures of (303.15 and 323.15) K and for pressures up to 980 kPa. The experimental uncertainties are estimated to be 10 mK for temperature, 0.45 kPa for pressure, (0.03 % + 0.005 kg·m<sup>-3</sup>) for density, and 0.31 % in mass fraction (0.32 % in mole fraction). The purities of propane and isobutane were both 99.99 % in mass fraction according to the report from the manufacturer. The measurements are used for assessing the reliability of existing equations of state.

## Introduction

For the development of energy-conversion systems, accurate thermodynamic properties of the working fluid are required. These properties are calculated from a thermodynamic equation of state. To develop the equations of state which accurately represent the gaseous thermodynamic surfaces of interest, reliable measurements of the thermodynamic properties must be available near saturation.

When the  $p\rho T_x$ -properties are not reported in the region near saturation in the gaseous phase, there is a possibility to have more than 5 % of uncertainty in the specific heat at saturation as we have found for R-143a.<sup>1</sup>

$p\rho T_x$ -properties of a system composed of propane + isobutane in the gaseous phase including in the region near saturation were measured with a magnetic suspension densimeter.

## Experimental Apparatus

An experimental apparatus which has two densimeters with a magnetic suspension balance was used for density measurements. The apparatus and the principle used here were reported by Wagner et al. in detail in a publication.<sup>2</sup>

Pressure was measured by a quartz digital pressure gauge, which was calibrated by using a dead-weight pressure gauge (model 5201, DH Instruments). The density measurement system consists of two magnetic suspension densimeters. The reliability was confirmed by the measurements of Argon density to be within (0.03 % + 0.005 kg·m<sup>-3</sup>) as reported in a previous publication.<sup>3</sup> The temperature was measured using a standard platinum-resistance thermometer. The temperature values were processed in accordance with the ITS-90. The thermometer was installed in the middle between the two cells of the A and B densimeters in the thermostatic bath.

The sample purities of propane and isobutane were better than 99.99 % in mass fraction according to the report from the manufacturer. Each sample was cooled by using liquid nitrogen

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**Table 1. Details of Temperature Uncertainty**

factor	uncertainty/mK
standard platinum resistance	1.0
thermometer bridge	0.27
temperature stability in the isothermal bath	3.0
temperature distribution in the isothermal bath	4.0
reproducibility of correlating equation by ITS-90	0.13
combined standard uncertainty	5.1
expanded uncertainty	10

**Table 2. Details of Pressure Uncertainty**

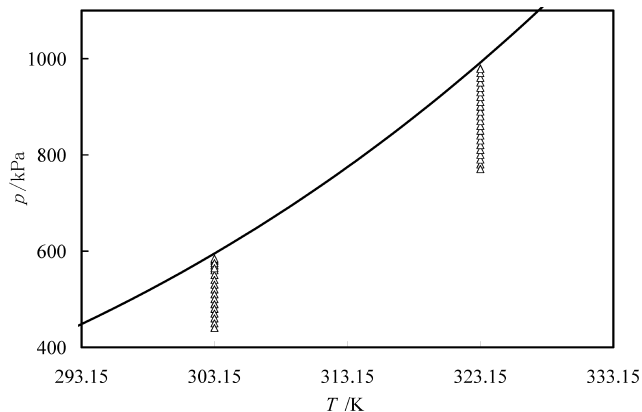
factor	uncertainty/kPa
quartz digital pressure gauge	0.098
variation of zero point	0.017
standard deviation of correlating equation	0.12
atmosphere pressure gauge	0.015
dead-weight pressure gauge	0.15
variation in measurements	0.06
pressure difference from head difference	0.033
combined standard uncertainty	0.23
expanded uncertainty	0.45

**Table 3. Filled Mass for Each Composition**

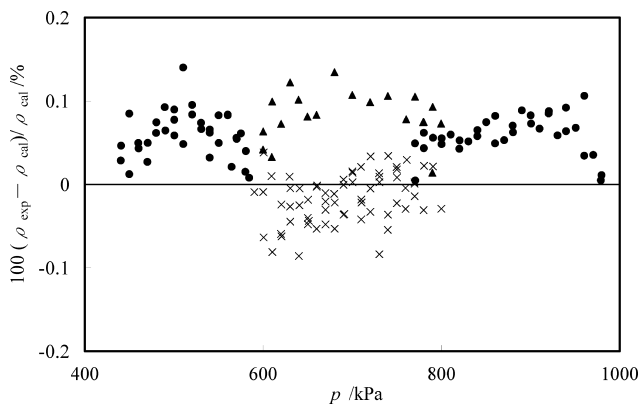
mole fraction of propane	filled mass/g	
	propane	isobutane
0.244	0.995	4.051
0.249	1.014	4.030
0.499	2.615	3.455
0.503	1.563	2.034
0.799	3.522	1.165

and then degassed once or twice using a vacuum pump. The weight of sample gases was measured by using a chemical balance.

The expanded uncertainties with a coverage factor of 2 having a level of confidence of 95 % were estimated to be not greater than 10 mK for temperature measurements, not greater than 0.45 kPa for pressure measurements, and not greater than (0.03 % + 0.005 kg·m<sup>-3</sup>) in density measurements. The composition measurement uncertainties were not greater than 0.31 % in mass fraction (0.32 % in mole fraction). Tables 1 and 2 show the details of the uncertainties in temperature and pressure measure-



**Figure 1.** Experimental data points for propane + isobutane mixtures at  $x_1 = 0.5$ .  $\Delta$ , This work. The line is the saturation curve calculated from ref. 6.



**Figure 2.** Relative deviation of the experimental density  $\rho_{\text{exp}}$  of propane + isobutane mixtures from values  $\rho_{\text{cal}}$  calculated from the equation of state developed by Kunz et al.<sup>6</sup>  $\times$ , This work ( $x_1 = 0.25$ );  $\bullet$ , This work ( $x_1 = 0.5$ );  $\blacktriangle$ , This work ( $x_1 = 0.80$ ).

**Table 4.** Details of Composition Uncertainty

mole fraction of propane	from purity of 99.99 %		mass measurement	residual mass in filling process	combined standard uncertainty	expanded uncertainty	expanded uncertainty
	propane	isobutane	g	g	mass fraction	mass fraction	mole fraction
	g	g					
0.244	0.0001	0.0004	0.006	0.005	0.0013	0.0026	0.0030
0.249	0.0001	0.0004			0.0013	0.0026	0.0030
0.499	0.0003	0.0004			0.0009	0.0018	0.0019
0.503	0.0002	0.0002			0.0015	0.0031	0.0032
0.799	0.0004	0.0001			0.0013	0.0026	0.0023

ments, respectively. Tables 3 and 4 show the filled mass of each composition and the details of composition measurement uncertainties, respectively.

## Experimental Results

The  $p\rho T$ -properties for propane + isobutane at  $x_1 = 0.25$  (65 points),  $x_1 = 0.5$  (69 points), and  $x_1 = 0.80$  (20 points) were represented along two different isotherms near saturation at temperatures of (303.15 and 323.15) K with pressures up to 980 kPa. The measured data for the mixture system of propane + isobutane are listed in Table 5. The data distribution exemplified at  $x_1 = 0.5$  is represented on a pressure–temperature plot in Figure 1. Our data were measured at every 10 kPa in the region near saturation. The reproducibility was confirmed by the data given at exactly the same state conditions.

## Discussion

An equation of state for propane has been developed by Lemmon et al.<sup>4</sup> and for isobutane by Buecker and Wagner.<sup>5</sup>

**Table 5.** Experimental  $p\rho T$ -Properties of Propane + Isobutane at  $x_1 = 0.25, 0.5$ , and  $0.80$

$x_1$	$T/\text{K}$	$p/\text{kPa}$	$\rho/\text{kg}\cdot\text{m}^{-3}$	$x_1$	$T/\text{K}$	$p/\text{kPa}$	$\rho/\text{kg}\cdot\text{m}^{-3}$
0.244	323.15	590.1	13.582	0.249	323.15	650.1	15.168
0.244	323.15	600.1	13.847	0.249	323.15	660.0	15.436
0.244	323.15	609.5	14.100	0.249	323.15	660.1	15.447
0.244	323.15	620.5	14.391	0.249	323.15	670.0	15.714
0.244	323.15	629.7	14.643	0.249	323.15	670.1	15.719
0.244	323.15	630.5	14.658	0.249	323.15	680.3	15.998
0.244	323.15	640.7	14.937	0.249	323.15	680.4	16.006
0.244	323.15	650.3	15.201	0.249	323.15	690.2	16.277
0.244	323.15	651.3	15.223	0.249	323.15	690.2	16.285
0.244	323.15	660.6	15.487	0.249	323.15	700.3	16.571
0.244	323.15	670.0	15.744	0.249	323.15	700.4	16.571
0.244	323.15	670.0	15.744	0.249	323.15	710.0	16.835
0.244	323.15	679.7	16.015	0.249	323.15	710.1	16.843
0.244	323.15	690.2	16.310	0.249	323.15	720.3	17.129
0.244	323.15	691.1	16.328	0.249	323.15	720.4	17.137
0.244	323.15	700.1	16.592	0.249	323.15	730.0	17.416
0.244	323.15	709.8	16.868	0.249	323.15	730.3	17.408
0.244	323.15	710.3	16.875	0.249	323.15	739.8	17.687
0.244	323.15	720.6	17.177	0.249	323.15	740.0	17.697
0.244	323.15	730.4	17.456	0.249	323.15	750.0	17.989
0.244	323.15	730.5	17.456	0.249	323.15	750.0	17.996
0.244	323.15	740.4	17.750	0.249	323.15	759.7	18.276
0.244	323.15	749.8	18.022	0.249	323.15	759.9	18.276
0.244	323.15	750.2	18.029	0.249	323.15	769.9	18.577
0.244	323.15	761.2	18.357	0.249	323.15	770.0	18.577
0.244	323.15	769.7	18.602	0.249	323.15	780.0	18.871
0.244	323.15	790.6	19.228	0.249	323.15	780.5	18.894
0.249	323.15	600.6	13.833	0.249	323.15	799.9	19.467
0.249	323.15	600.7	13.848	0.499	323.15	770.4	16.983
0.249	323.15	610.4	14.090	0.499	323.15	770.7	16.982
0.249	323.15	620.1	14.354	0.499	323.15	780.2	17.239
0.249	323.15	620.7	14.369	0.499	323.15	780.3	17.244
0.249	323.15	630.3	14.633	0.499	323.15	790.6	17.513
0.249	323.15	630.5	14.640	0.499	323.15	800.2	17.765
0.249	323.15	640.1	14.889	0.499	323.15	800.2	17.769
0.249	323.15	640.9	14.923	0.499	323.15	810.5	18.042
0.249	323.15	650.1	15.168	0.499	323.15	820.2	18.299
0.499	323.15	820.4	18.307	0.503	303.15	510.3	11.608
0.499	323.15	830.3	18.572	0.503	303.15	510.5	11.600
0.499	323.15	840.3	18.844	0.503	303.15	520.4	11.861
0.499	323.15	840.4	18.848	0.503	303.15	520.4	11.864
0.499	323.15	850.3	19.121	0.503	303.15	530.4	12.121
0.499	323.15	860.2	19.387	0.503	303.15	530.7	12.129
0.499	323.15	860.4	19.398	0.503	303.15	540.1	12.370
0.499	323.15	870.4	19.669	0.503	303.15	540.2	12.378
0.499	323.15	879.9	19.938	0.503	303.15	540.2	12.378
0.499	323.15	880.4	19.948	0.503	303.15	550.1	12.642
0.499	323.15	890.2	20.228	0.503	303.15	550.3	12.642
0.499	323.15	900.1	20.506	0.503	303.15	560.3	12.914
0.499	323.15	900.6	20.517	0.503	303.15	560.3	12.914
0.499	323.15	910.1	20.784	0.503	303.15	564.6	13.019
0.499	323.15	920.3	21.078	0.503	303.15	570.1	13.170
0.499	323.15	920.6	21.087	0.503	303.15	570.4	13.178
0.499	323.15	930.3	21.359	0.503	303.15	575.1	13.306
0.499	323.15	939.7	21.637	0.503	303.15	580.1	13.434
0.499	323.15	939.8	21.635	0.503	303.15	580.7	13.453
0.499	323.15	950.6	21.949	0.503	303.15	584.3	13.548
0.499	323.15	960.2	22.222	0.799	303.15	599.9	12.550
0.499	323.15	960.3	22.242	0.799	303.15	600.1	12.557
0.499	323.15	970.3	22.521	0.799	303.15	609.7	12.784
0.499	323.15	978.9	22.767	0.799	303.15	610.2	12.802
0.499	323.15	979.6	22.791	0.799	303.15	620.2	13.040
0.503	303.15	440.3	9.824	0.799	303.15	630.2	13.289
0.503	303.15	440.7	9.834	0.799	303.15	639.7	13.516
0.503	303.15	449.9	10.061	0.799	303.15	649.7	13.757
0.503	303.15	450.0	10.069	0.799	303.15	659.8	14.006
0.503	303.15	460.0	10.317	0.799	303.15	680.1	14.516
0.503	303.15	460.4	10.325	0.799	303.15	700.0	15.010
0.503	303.15	470.2	10.570	0.799	303.15	720.0	15.515
0.503	303.15	470.5	10.581	0.799	303.15	739.9	16.028
0.503	303.15	480.0	10.823	0.799	303.15	760.5	16.557
0.503	303.15	480.3	10.830	0.799	303.15	770.4	16.821
0.503	303.15	489.7	11.072	0.799	303.15	779.5	17.055
0.503	303.15	490.4	11.087	0.799	303.15	780.1	17.073
0.503	303.15	500.3	11.344	0.799	303.15	789.8	17.319
0.503	303.15	500.4	11.344	0.799	303.15	790.1	17.342
0.503	303.15	500.4	11.344	0.799	303.15	799.6	17.590

The equation of state for the properties of the mixture developed by Kunz et al.<sup>6</sup> is applied, and the relative deviations of the experimental data of this work from the calculated values are presented in Figure 2. As shown in Figure 2, the discrepancy between our data and the equation of state developed by Kunz et al. is between (−0.1 and 0.15) % depending on the composition.

### Conclusions

The  $p\rho T$ -properties of propane (1) and isobutane (2) mixtures in the gaseous phase including values near saturation were measured with a magnetic suspension densimeter. A total of 154  $p\rho T$ -values at  $x_1 = 0.25, 0.5, \text{ and } 0.80$  with an uncertainty of  $(0.03\% + 0.005 \text{ kg}\cdot\text{m}^{-3})$  in density were obtained. In the near future, reliable values of the virial coefficient values and of other thermodynamic properties such as specific heats, sound speed, etc. including those near saturation conditions or at very low pressures, where measurements are not easily performed, will be calculated on the basis of the present data.

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